



## **RESEARCH REPORT**

การประมาณค่าจุดเปลี่ยนในตัวแบบถดถอย โทบิต-พีซไวส์

**AN ESTIMATION OF A JOINED POINT IN  
TOBIT-PIECEWISE REGRESSION MODEL**

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